## ECONOMICS 6002 CLASS 22 LIMITED DEPENDENT VARIABLE MODELS

- 1. Limited dependent variables are subject to an upper and/or lower limit on their allowable range.
  - a. Truncation: sample is limited to values satisfying the limit(s)
  - b. Censoring: values beyond the limit are set at the limit
- 2. Truncation
  - a. Truncated values can be estimated through the specification of a distribution function for the disturbances - usually normal for continuous variables and Poisson for count data
  - b. Estimation can be done through maximum likelihood
  - c. Regression suffers from an omitted variable problem, and is inconsistent
- 3. Sample Selection and Incidental truncation
  - a. Omitted variable bias from sample-selection
  - b. Estimation via Heckman two-step ("Heckit") procedure
    - i. Estimate selection equation by maximum likelihood
    - ii. Calculate truncation bias variable from estimate of selection equation
    - iii. Estimate incidentally truncated equation augmented by truncation bias variable using OLS or GLS.
- 4. Censoring
  - a. A censored variable is distributed normally (continuously) at non-limit points, but has a discrete distribution (similar to a discrete-choice model) at a limit point.
  - b. The Tobit ("Tobin's probit") model estimates through maximum likelihood, with a normal likelihood for the non-limit observations and a probit likelihood function for the limit observations.
  - c. As usual, the ML estimates are consistent only if the distributional assumptions (e.g., normality, homoskedasticity) are consistent with the data.
  - d. If the limit and non-limit observations are drawn from different distributions, the model can be estimated by
    - i. Specifying a probit model for the limit observations, and
    - ii. A truncated distribution for the non-limit observations

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