

ECONOMICS 6002 CLASSES 3-4
BASIC STATISTICAL INFERENCE UNDER ORDINARY LEAST SQUARES

1. Testing a hypothesis about a coefficient - the t test
 - a. Testing statistical significance: $H_0 : \beta=0$
 - i. Role of the normality assumption
 - ii. Distribution of the t -statistic
 - b. Testing hypotheses on coefficients $H_0 : \beta=c$
 - c. Testing linear combinations of coefficients . $H_0: r'\beta = q$
 - d. Estimating the variances and covariances of OLS estimates
 - i. $\text{cov}(\beta) = \sigma^2 (X'X)^{-1}$
 - ii. Estimating σ^2

2. Testing joint hypotheses: e.g. $H_0: \{ \beta_1 = 0, \beta_2 = 0 \}$ - the F test
 - a. Motivation: estimates of β_1 and β_2 can be correlated
 - b. Distribution of the F -statistic
 - c. General form: $H_0: R'\beta = q, R \text{ JxK}$
 - d. The F test is a test on $[SSE_R - SSE_U]$ - R =restricted, U =unrestricted

3. Testing non-linear hypotheses - the Wald test W
 - a. t and F tests cannot test *non-linear* hypotheses - not normally distributed
 - b. W can be used to test *non-linear* hypotheses
 - i. Relies on consistency and the Central Limit Theorem, so is only an **asymptotic** test
 - ii. Estimation of the asymptotic variance of a non-linear function
 - c. W can test both simple and joint hypotheses
 - d. W is distributed (asymptotically) as chi-squared
 - e. W is valid (asymptotically) even when disturbances are **not** normally distributed